

Quantifying equiaxed versus epitaxial solidification in laser melting of CMSX-4 single crystal superalloy

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Motivation

Mixture of Columnar and Equiaxed Grains



Mokadem et al., Solidification and Microstructure, (2004)

- New grains with orientation different from the base material were often found in welding repaired nickelbased single-crystal superalloys
- Adjusting printing parameters are proven to be effective in mitigating stray grains formation
- Extend the parameters to LPBF conditions

Methods

Analytical solidification modeling based on constitutional undercooling

Temperature

$$T_0 + rac{\eta P}{2\pi k\sqrt{x^2 + y^2 + z^2}} \exp\left[rac{-V(\sqrt{x^2 + y^2 + z^2} - 2\alpha)}{2\alpha}\right]$$

Thermal gradient
$$G = |\nabla T| = \left| \frac{\partial T}{\partial x} \hat{i} + \frac{\partial T}{\partial y} \hat{j} + \frac{\partial T}{\partial z} \hat{k} \right| = \sqrt{\left(\frac{\partial T}{\partial x} \right)^2 + \left(\frac{\partial T}{\partial y} \right)^2 + \left(\frac{\partial T}{\partial z} \right)^2}$$

Solidification Isotherm Velocity

T =

$$v_T = V \cos \theta = V \frac{\frac{\partial T}{\partial x}}{\sqrt{\left(\frac{\partial T}{\partial x}\right)^2 + \left(\frac{\partial T}{\partial y}\right)^2 + \left(\frac{\partial T}{\partial z}\right)^2}}$$

Local Stray Grain Area Fraction

$$\Phi = 1 - e^{S}$$

where $S = \frac{-4\pi N_0}{3} \left(\frac{1}{(n+1)(G^n/av_T)^{1/n}} \right)^3 = -2.356 \times 10^{19} \left(\frac{v_T}{G^{3.4}} \right)^{\frac{3}{3.4}}$

Computational fluid dynamics (CFD)

Recoil Pressure

$$\Pr \cong 0.54 P_0 \exp\left(\Delta H_{\rm LV} \frac{T - T_{\rm LV}}{RT T_{\rm LV}}\right)$$

Surface tension coefficient including Marangoni flow $\sigma = 1.79 - 9.90 \cdot 10^{-4} (T - 1654K) \text{ Nm}^{-1}$

Vitek, The sixth internation EPRI conference, (2004) Cho et al., *Journal of Physics D*, (2006)



